Discussiones Mathematicae
General Algebra and Applications 38 (2018) 239–241
doi:10.7151/dmgaa.1296

BI-INTERIOR IDEALS OF Γ-SEMIRINGS

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Abstract

In this paper, as a further generalization of ideals, we introduce the notion of bi-interior ideal as a generalization of quasi ideal, bi-ideal and interior ideal of Γ-semiring and study the properties of bi-interior ideals of Γ-semiring. We prove that if M is a field Γ-semiring, then M is a bi-interior simple Γ-semiring.

Keywords: quasi ideal, bi-ideal, interior ideal, bi-interior ideal, bi-quasi ideal, regular Γ-semiring, bi-interior simple Γ-semiring.

2010 Mathematics Subject Classification: 16Y60, 06Y99.

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Received 19 April 2018
Revised 9 August 2018
Accepted 4 Septemeber 2018