

TRACE INEQUALITIES FOR POSITIVE SEMIDEFINITE MATRICES

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AND

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Abstract

Certain trace inequalities for positive definite matrices are generalized for positive semidefinite matrices using the notion of the group generalized inverse.

Keywords: positive semidefinite matrix, group inverse, trace inequalities.

2010 Mathematics Subject Classification: 15B57, 15A09, 15A39.

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Received 18 December 2016

Revised 8 February 2017