

## ALL MAXIMAL COMPLETELY REGULAR SUBMONOIDS OF $Hyp_G(2)$

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AND

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### Abstract

In this paper we consider mappings  $\sigma$  which map the binary operation symbol  $f$  to the term  $\sigma(f)$  which do not necessarily preserve the arity. These mappings are called generalized hypersubstitutions of type  $\tau = (2)$  and we denote the set of all these generalized hypersubstitutions of type  $\tau = (2)$  by  $Hyp_G(2)$ . The set  $Hyp_G(2)$  together with a binary operation defined on this set and the identity generalized hypersubstitution which maps  $f$  to the term  $f(x_1, x_2)$  forms a monoid. In this paper, we determine all maximal completely regular submonoids of this monoid.

**Keywords:** generalized hypersubstitution, regular element, completely regular.

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