

ON THE LENGTH OF RATIONAL CONTINUED FRACTIONS OVER $\mathbb{F}_q(X)$

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Abstract

Let \mathbb{F}_q be a finite field and $A(Y) \in \mathbb{F}_q(X, Y)$. The aim of this paper is to prove that the length of the continued fraction expansion of $A(P); P \in \mathbb{F}_q[X]$, is bounded.

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