

INTERVALS OF CERTAIN CLASSES OF Z -MATRICES

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Abstract

Let A and B be M -matrices satisfying $A \leq B$ and $J = [A, B]$ be the set of all matrices C such that $A \leq C \leq B$, where the order is component wise. It is rather well known that if A is an M -matrix and B is an invertible M -matrix and $A \leq B$, then $aA + bB$ is an invertible M -matrix for all $a, b > 0$. In this article, we present an elementary proof of a stronger version of this result and study corresponding results for certain other classes as well.

Keywords: interval matrix, M -matrix, N -matrix, N_0 -matrix, nonnegativity.

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