

FUZZY n -FOLD INTEGRAL FILTERS IN *BL*-ALGEBRAS

RAJAB ALI BORZOOEI

*Department of Mathematics
Shahid Beheshti University
Tehran, Iran*

e-mail: borzooei@sbu.ac.ir

AND

AKBAR PAAD

*Department of Mathematics
Shahid Beheshti University Tehran, Iran*

e-mail: Akbar.Paad@gmail.com

Abstract

In this paper, we introduce the notion of fuzzy n -fold integral filter in *BL*-algebras and we state and prove several properties of fuzzy n -fold integral filters. Using a level subset of a fuzzy set in a *BL*-algebra, we give a characterization of fuzzy n -fold integral filters. Also, we prove that the homomorphic image and preimage of fuzzy n -fold integral filters are also fuzzy n -fold integral filters. Finally, we study the relationship among fuzzy n -fold obstinate filters, fuzzy n -fold integral filters and fuzzy n -fold fantastic filters.

Keywords: *BL*-algebra, fuzzy n -fold obstinate filter, n -fold obstinate *BL*-algebra, n -fold integral *BL*-algebra and fuzzy n -fold integra filter.

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