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L-ZERO-DIVISOR GRAPHS OF DIRECT PRODUCTS OF L-COMMUTATIVE RINGS

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Abstract

L-zero-divisor graphs of L-commutative rings have been introduced and studied in [5]. Here we consider L-zero-divisor graphs of a finite direct product of L-commutative rings. Specifically, we look at the preservation, or lack thereof, of the diameter and girth of the L-ziro-divisor graph of a L-ring when extending to a finite direct product of L-commutative rings.

Keywords: μ-zero-divisor, L-zero-divisor graph, μ-diameter, μ-girth, finite direct products.

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