

## POSITIVE SPLITTINGS OF MATRICES AND THEIR NONNEGATIVE MOORE-PENROSE INVERSES

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### Abstract

In this short note we study necessary and sufficient conditions for the nonnegativity of the Moore-Penrose inverse of a real matrix in terms of certain spectral property shared by all positive splittings of the given matrix.

**Keywords:** Moore-Penrose inverse, positive splitting.

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